

Mathematical Operators

Range: 2200–22FF

This file contains an excerpt from the character code tables and list of character names for the Unicode Standard, last updated for *The Unicode Standard, Version 4.0*.

This file may be updated as necessary to reflect errata without notice. For an up-to-date list of errata, see <http://www.unicode.org/errata/>

Disclaimer

These charts are provided as the on-line reference to the character contents of the Unicode Standard, Version 4.0 but do not provide all the information needed to fully support individual scripts using the Unicode Standard. For a complete understanding of the use of the characters contained in this excerpt file, please consult the appropriate sections of *The Unicode Standard, Version 4.0* (ISBN 0-321-18578-1), as well as Unicode Standard Annexes #9, #11, #14, #15, #24 and #29, the other Unicode Technical Reports and the Unicode Character Database, which are available on-line.

See <http://www.unicode.org/Public/UNIDATA/UCD.html> and <http://www.unicode.org/reports/>

A thorough understanding of the information contained in these additional sources is required for a successful implementation.

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See <http://www.unicode.org/pending/pending.html> and <http://www.unicode.org/alloc/Pipeline.html>.

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	220	221	222	223	224	225	226	227	228	229	22A	22B	22C	22D	22E	22F
0	2200	2210	2220	2230	2240	2250	2260	2270	2280	2290	22A0	22B0	22C0	22D0	22E0	22F0
1	2201	2211	2221	2231	2241	2251	2261	2271	2281	2291	22A1	22B1	22C1	22D1	22E1	22F1
2	2202	2212	2222	2232	2242	2252	2262	2272	2282	2292	22A2	22B2	22C2	22D2	22E2	22F2
3	2203	2213	2223	2233	2243	2253	2263	2273	2283	2293	22A3	22B3	22C3	22D3	22E3	22F3
4	2204	2214	2224	2234	2244	2254	2264	2274	2284	2294	22A4	22B4	22C4	22D4	22E4	22F4
5	2205	2215	2225	2235	2245	2255	2265	2275	2285	2295	22A5	22B5	22C5	22D5	22E5	22F5
6	2206	2216	2226	2236	2246	2256	2266	2276	2286	2296	22A6	22B6	22C6	22D6	22E6	22F6
7	2207	2217	2227	2237	2247	2257	2267	2277	2287	2297	22A7	22B7	22C7	22D7	22E7	22F7
8	2208	2218	2228	2238	2248	2258	2268	2278	2288	2298	22A8	22B8	22C8	22D8	22E8	22F8
9	2209	2219	2229	2239	2249	2259	2269	2279	2289	2299	22A9	22B9	22C9	22D9	22E9	22F9
A	220A	221A	222A	223A	224A	225A	226A	227A	228A	229A	22AA	22BA	22CA	22DA	22EA	22FA
B	220B	221B	222B	223B	224B	225B	226B	227B	228B	229B	22AB	22BB	22CB	22DB	22EB	22FB
C	220C	221C	222C	223C	224C	225C	226C	227C	228C	229C	22AC	22BC	22CC	22DC	22EC	22FC
D	220D	221D	222D	223D	224D	225D	226D	227D	228D	229D	22AD	22BD	22CD	22DD	22ED	22FD
E	220E	221E	222E	223E	224E	225E	226E	227E	228E	229E	22AE	22BE	22CE	22DE	22EE	22FE
F	220F	221F	222F	223F	224F	225F	226F	227F	228F	229F	22AF	22BF	22CF	22DF	22EF	22FF

Mathematical operators

2200	∀	FOR ALL	2215	/	DIVISION SLASH • generic division operator → 002F / solidus → 2044 / fraction slash
2201	⊂	COMPLEMENT → 0297 ⊂ latin letter stretched c	2216	∖	SET MINUS → 005C ∖ reverse solidus
2202	∂	PARTIAL DIFFERENTIAL	2217	*	ASTERISK OPERATOR → 002A * asterisk
2203	∃	THERE EXISTS	2218	∘	RING OPERATOR = composite function = APL jot → 00B0 ° degree sign → 25E6 ∘ white bullet
2204	∄	THERE DOES NOT EXIST ≡ 2203 ∃ 0338 ∄	2219	•	BULLET OPERATOR → 00B7 • middle dot → 2022 • bullet → 2024 . one dot leader
2205	∅	EMPTY SET = null set → 00D8 Ø latin capital letter o with stroke → 2300 ∅ diameter sign	221A	√	SQUARE ROOT = radical sign → 2713 ✓ check mark
2206	Δ	INCREMENT = Laplace operator = forward difference → 0394 Δ greek capital letter delta → 25B3 △ white up-pointing triangle	221B	∛	CUBE ROOT
2207	∇	NABLA = Laplace operator (written with superscript 2) = backward difference = del → 25BD ∇ white down-pointing triangle	221C	∜	FOURTH ROOT
2208	∈	ELEMENT OF	221D	∝	PROPORTIONAL TO → 03B1 α greek small letter alpha
2209	∉	NOT AN ELEMENT OF ≡ 2208 ∈ 0338 ∄	221E	∞	INFINITY
220A	∈	SMALL ELEMENT OF • originates in math pi fonts; not the straight epsilon → 03F5 ∈ greek lunate epsilon symbol	221F	⊥	RIGHT ANGLE
220B	⊃	CONTAINS AS MEMBER = such that	2220	∠	ANGLE
220C	⊄	DOES NOT CONTAIN AS MEMBER ≡ 220B ⊃ 0338 ∄	2221	∠	MEASURED ANGLE
220D	⊃	SMALL CONTAINS AS MEMBER → 03F6 ⊃ greek reversed lunate epsilon symbol	2222	∠	SPHERICAL ANGLE = angle arc
220E	■	END OF PROOF = Q.E.D. → 2023 ▶ triangular bullet → 25AE ■ black vertical rectangle	2223		DIVIDES = such that = APL stile → 007C vertical line → 01C0 latin letter dental click
220F	∏	N-ARY PRODUCT = product sign → 03A0 ∏ greek capital letter pi	2224	∤	DOES NOT DIVIDE ≡ 2223 0338 ∄
2210	∏	N-ARY COPRODUCT = coproduct sign	2225	∥	PARALLEL TO → 01C1 ∥ latin letter lateral click → 2016 ∥ double vertical line
2211	∑	N-ARY SUMMATION = summation sign → 03A3 ∑ greek capital letter sigma	2226	∦	NOT PARALLEL TO ≡ 2225 ∥ 0338 ∄
2212	-	MINUS SIGN → 002D - hyphen-minus	2227	∧	LOGICAL AND = wedge, conjunction → 22C0 ∧ n-ary logical and → 2303 ^ up arrowhead
2213	±	MINUS-OR-PLUS SIGN → 00B1 ± plus-minus sign	2228	∨	LOGICAL OR = vee, disjunction → 22C1 ∨ n-ary logical or → 2304 ∨ down arrowhead
2214	+	DOT PLUS	2229	∩	INTERSECTION = cap, hat → 22C2 ∩ n-ary intersection
			222A	∪	UNION = cup → 22C3 ∪ n-ary union

222B	\int INTEGRAL → 0283 \int latin small letter esh	2247	\neq NEITHER APPROXIMATELY NOR ACTUALLY EQUAL TO ≡ 2245 ≡ 0338 \neq
222C	\iint DOUBLE INTEGRAL ≈ 222B \int 222B \int	2248	\approx ALMOST EQUAL TO = asymptotic to
222D	\iiint TRIPLE INTEGRAL → 2A0C \iiint quadruple integral operator ≈ 222B \int 222B \int 222B \int	2249	$\not\approx$ NOT ALMOST EQUAL TO ≡ 2248 ≈ 0338 \neq
222E	\oint CONTOUR INTEGRAL → 2A15 \oint integral around a point operator	224A	\cong ALMOST EQUAL OR EQUAL TO
222F	\oiint SURFACE INTEGRAL ≈ 222E \oint 222E \oint	224B	\equiv TRIPLE TILDE
2230	\iiint VOLUME INTEGRAL ≈ 222E \oint 222E \oint 222E \oint	224C	\equiv ALL EQUAL TO • reversed tilde and lazy S are glyph variants
2231	\int CLOCKWISE INTEGRAL	224D	\asymp EQUIVALENT TO
2232	\oint CLOCKWISE CONTOUR INTEGRAL	224E	\simeq GEOMETRICALLY EQUIVALENT TO
2233	\oint ANTICLOCKWISE CONTOUR INTEGRAL • clockwise or anticlockwise arrows do not reverse during layout mirroring	224F	\simeq DIFFERENCE BETWEEN
2234	\therefore THEREFORE	2250	\doteq APPROACHES THE LIMIT
2235	\because BECAUSE	2251	\doteq GEOMETRICALLY EQUAL TO
2236	$:$ RATIO → 003A $:$ colon	2252	\doteq APPROXIMATELY EQUAL TO OR THE IMAGE OF = nearly equals
2237	\therefore PROPORTION	2253	\doteq IMAGE OF OR APPROXIMATELY EQUAL TO
2238	$\dot{-}$ DOT MINUS = symmetric difference	2254	\doteq COLON EQUALS
2239	\therefore EXCESS	2255	\doteq EQUALS COLON
223A	\doteq GEOMETRIC PROPORTION	2256	\doteq RING IN EQUAL TO
223B	\doteq HOMOTHETIC → 2A6B \doteq tilde operator with rising dots	2257	\doteq RING EQUAL TO = approximately equal to
223C	\sim TILDE OPERATOR = varies with (proportional to) = difference between = similar to = not = cycle = APL tilde → 007E \sim tilde → 00AC \sim not sign → 02DC \sim small tilde	2258	\doteq CORRESPONDS TO
223D	$\bar{\smile}$ REVERSED TILDE = lazy S • reversed tilde and lazy S are glyph variants	2259	\doteq ESTIMATES = corresponds to
223E	\smile INVERTED LAZY S = most positive	225A	\doteq EQUIANGULAR TO
223F	\sim SINE WAVE = alternating current	225B	\doteq STAR EQUALS
2240	\wr WREATH PRODUCT	225C	\doteq DELTA EQUAL TO = equiangular = equal to by definition
2241	\nexists NOT TILDE ≡ 223C \sim 0338 \neq	225D	\doteq EQUAL TO BY DEFINITION
2242	\neq MINUS TILDE	225E	\doteq MEASURED BY
2243	\approx ASYMPTOTICALLY EQUAL TO	225F	\doteq QUESTIONED EQUAL TO
2244	$\not\approx$ NOT ASYMPTOTICALLY EQUAL TO ≡ 2243 ≈ 0338 \neq	2260	\neq NOT EQUAL TO → 003D = equals sign → 01C2 \neq latin letter alveolar click ≡ 003D = 0338 \neq
2245	\cong APPROXIMATELY EQUAL TO	2261	\equiv IDENTICAL TO
2246	\cong APPROXIMATELY BUT NOT ACTUALLY EQUAL TO	2262	$\not\equiv$ NOT IDENTICAL TO ≡ 2261 ≡ 0338 \neq
		2263	\equiv STRICTLY EQUIVALENT TO
		2264	\leq LESS-THAN OR EQUAL TO
		2265	\geq GREATER-THAN OR EQUAL TO
		2266	\leq LESS-THAN OVER EQUAL TO
		2267	\geq GREATER-THAN OVER EQUAL TO
		2268	\leq LESS-THAN BUT NOT EQUAL TO
		2269	\geq GREATER-THAN BUT NOT EQUAL TO
		226A	\ll MUCH LESS-THAN → 00AB \ll left-pointing double angle quotation mark
		226B	\gg MUCH GREATER-THAN → 00BB \gg right-pointing double angle quotation mark

226C	∅	BETWEEN = plaintiff, quantic	2289	⊇	NEITHER A SUPERSET OF NOR EQUAL TO ≡ 2287 ⊇ 0338 ∅
226D	≠	NOT EQUIVALENT TO ≡ 224D ≠ 0338 ∅	228A	⊆	SUBSET OF WITH NOT EQUAL TO
226E	≠	NOT LESS-THAN ≡ 003C < 0338 ∅	228B	⊇	SUPERSET OF WITH NOT EQUAL TO
226F	≠	NOT GREATER-THAN ≡ 003E > 0338 ∅	228C	∪	MULTISET
2270	≠	NEITHER LESS-THAN NOR EQUAL TO ≡ 2264 ≤ 0338 ∅	228D	∪	MULTISET MULTIPLICATION → 2A03 ∪ n-ary union operator with dot → 2A40 ∩ intersection with dot
2271	≠	NEITHER GREATER-THAN NOR EQUAL TO ≡ 2265 ≥ 0338 ∅	228E	∪	MULTISET UNION = z notation bag addition → 2A04 ∪ n-ary union operator with plus
2272	≠	LESS-THAN OR EQUIVALENT TO	228F	□	SQUARE IMAGE OF
2273	≠	GREATER-THAN OR EQUIVALENT TO	2290	□	SQUARE ORIGINAL OF
2274	≠	NEITHER LESS-THAN NOR EQUIVALENT TO ≡ 2272 ≤ 0338 ∅	2291	□	SQUARE IMAGE OF OR EQUAL TO
2275	≠	NEITHER GREATER-THAN NOR EQUIVALENT TO ≡ 2273 ≥ 0338 ∅	2292	□	SQUARE ORIGINAL OF OR EQUAL TO
2276	≠	LESS-THAN OR GREATER-THAN	2293	□	SQUARE CAP → 2A05 □ n-ary square intersection operator
2277	≠	GREATER-THAN OR LESS-THAN	2294	□	SQUARE CUP
2278	≠	NEITHER LESS-THAN NOR GREATER- THAN ≡ 2276 ≤ 0338 ∅	2295	⊕	CIRCLED PLUS = direct sum = vector pointing into page → 2641 Ⓢ earth → 2A01 ⊕ n-ary circled plus operator
2279	≠	NEITHER GREATER-THAN NOR LESS- THAN ≡ 2277 ≥ 0338 ∅	2296	⊖	CIRCLED MINUS = symmetric difference → 29B5 ⊖ circle with horizontal bar
227A	<	PRECEDES = lower rank than → 22B0 ≪ precedes under relation	2297	⊗	CIRCLED TIMES = tensor product = vector pointing into page → 2A02 ⊗ n-ary circled times operator
227B	>	SUCCEEDS = higher rank than → 22B1 ≻ succeeds under relation	2298	⊘	CIRCLED DIVISION SLASH
227C	≠	PRECEDES OR EQUAL TO	2299	⊙	CIRCLED DOT OPERATOR = direct product = vector pointing out of page → 0298 ⊙ latin letter bilabial click → 2609 ⊙ sun → 2A00 ⊙ n-ary circled dot operator
227D	≠	SUCCEEDS OR EQUAL TO	229A	⊚	CIRCLED RING OPERATOR → 233E ⊚ apl functional symbol circle jot → 25CE ⊚ bullseye
227E	≠	PRECEDES OR EQUIVALENT TO	229B	⊛	CIRCLED ASTERISK OPERATOR → 235F ⊛ apl functional symbol circle star
227F	≠	SUCCEEDS OR EQUIVALENT TO	229C	⊜	CIRCLED EQUALS
2280	≠	DOES NOT PRECEDE ≡ 227A < 0338 ∅	229D	⊝	CIRCLED DASH
2281	≠	DOES NOT SUCCEED ≡ 227B > 0338 ∅	229E	⊞	SQUARED PLUS
2282	⊆	SUBSET OF = included in set	229F	⊟	SQUARED MINUS
2283	⊇	SUPERSET OF = includes in set	22A0	⊠	SQUARED TIMES → 2612 ⊠ ballot box with x
2284	⊈	NOT A SUBSET OF ≡ 2282 ⊆ 0338 ∅	22A1	⊡	SQUARED DOT OPERATOR
2285	⊉	NOT A SUPERSET OF ≡ 2283 ⊇ 0338 ∅	22A2	⊢	RIGHT TACK = turnstile = proves, implies, yields = reducible
2286	⊆	SUBSET OF OR EQUAL TO	22A3	⊣	LEFT TACK = reverse turnstile = non-theorem, does not yield
2287	⊇	SUPERSET OF OR EQUAL TO			
2288	⊈	NEITHER A SUBSET OF NOR EQUAL TO ≡ 2286 ⊆ 0338 ∅			

22A4	⊥	DOWN TACK = top	22C2	∩	N-ARY INTERSECTION = z notation generalised intersection → 2229 ∩ intersection
22A5	⊥	UP TACK = orthogonal to = perpendicular = base, bottom	22C3	∪	N-ARY UNION = z notation generalised union → 222A ∪ union
22A6	⊢	ASSERTION = reduces to	22C4	◊	DIAMOND OPERATOR → 25C7 ◊ white diamond
22A7	⊨	MODELS	22C5	⋅	DOT OPERATOR → 00B7 ⋅ middle dot
22A8	⊨	TRUE = statement is true, valid = is a tautology = satisfies = results in	22C6	*	STAR OPERATOR • APL → 066D * arabic five pointed star → 2605 ★ black star
22A9	⊨	FORCES	22C7	∗	DIVISION TIMES
22AA	≡	TRIPLE VERTICAL BAR RIGHT TURNSTILE	22C8	⌘	BOWTIE → 2445 ⌘ ocr bow tie
22AB	≡	DOUBLE VERTICAL BAR DOUBLE RIGHT TURNSTILE	22C9	⋈	LEFT NORMAL FACTOR SEMIDIRECT PRODUCT
22AC	⊄	DOES NOT PROVE ≡ 22A2 ⊢ 0338 ∅	22CA	⋈	RIGHT NORMAL FACTOR SEMIDIRECT PRODUCT
22AD	⊄	NOT TRUE ≡ 22A8 ⊨ 0338 ∅	22CB	⋈	LEFT SEMIDIRECT PRODUCT
22AE	⊄	DOES NOT FORCE ≡ 22A9 ⊨ 0338 ∅	22CC	⋈	RIGHT SEMIDIRECT PRODUCT → 2041 ⋈ caret insertion point
22AF	≡	NEGATED DOUBLE VERTICAL BAR DOUBLE RIGHT TURNSTILE ≡ 22AB ≡ 0338 ∅	22CD	≈	REVERSED TILDE EQUALS
22B0	⋈	PRECEDES UNDER RELATION → 227A < precedes	22CE	∨	CURLY LOGICAL OR
22B1	⋈	SUCCEEDS UNDER RELATION → 227B > succeeds	22CF	∧	CURLY LOGICAL AND
22B2	⋈	NORMAL SUBGROUP OF → 25C5 ⋈ white left-pointing pointer	22D0	⊆	DOUBLE SUBSET
22B3	⋈	CONTAINS AS NORMAL SUBGROUP → 25BB ⋈ white right-pointing pointer	22D1	⊇	DOUBLE SUPERSET
22B4	⋈	NORMAL SUBGROUP OF OR EQUAL TO	22D2	∩	DOUBLE INTERSECTION
22B5	⋈	CONTAINS AS NORMAL SUBGROUP OR EQUAL TO	22D3	∪	DOUBLE UNION
22B6	↔	ORIGINAL OF	22D4	∩	PITCHFORK = proper intersection
22B7	↔	IMAGE OF	22D5	#	EQUAL AND PARALLEL TO → 2317 # viewdata square
22B8	→	MULTIMAP	22D6	<	LESS-THAN WITH DOT
22B9	÷	HERMITIAN CONJUGATE MATRIX	22D7	>	GREATER-THAN WITH DOT
22BA	⊥	INTERCALATE	22D8	≪	VERY MUCH LESS-THAN
22BB	⊕	XOR	22D9	≫	VERY MUCH GREATER-THAN
22BC	⊖	NAND → 2305 ⊖ projective	22DA	≧	LESS-THAN EQUAL TO OR GREATER- THAN
22BD	∇	NOR	22DB	≧	GREATER-THAN EQUAL TO OR LESS- THAN
22BE	⊥	RIGHT ANGLE WITH ARC	22DC	≥	EQUAL TO OR LESS-THAN
22BF	⊥	RIGHT TRIANGLE	22DD	≥	EQUAL TO OR GREATER-THAN
22C0	∧	N-ARY LOGICAL AND → 2227 ∧ logical and	22DE	≤	EQUAL TO OR PRECEDES
22C1	∨	N-ARY LOGICAL OR → 2228 ∨ logical or	22DF	≥	EQUAL TO OR SUCCEEDS
			22E0	≠	DOES NOT PRECEDE OR EQUAL ≡ 227C ≤ 0338 ∅
			22E1	≠	DOES NOT SUCCEED OR EQUAL ≡ 227D ≥ 0338 ∅
			22E2	⊈	NOT SQUARE IMAGE OF OR EQUAL TO ≡ 2291 ⊈ 0338 ∅
			22E3	⊈	NOT SQUARE ORIGINAL OF OR EQUAL TO ≡ 2292 ⊈ 0338 ∅

22E4	⊐	SQUARE IMAGE OF OR NOT EQUAL TO
22E5	⊑	SQUARE ORIGINAL OF OR NOT EQUAL TO
22E6	≍	LESS-THAN BUT NOT EQUIVALENT TO
22E7	≎	GREATER-THAN BUT NOT EQUIVALENT TO
22E8	⋈	PRECEDES BUT NOT EQUIVALENT TO
22E9	⋉	SUCCEEDS BUT NOT EQUIVALENT TO
22EA	⊈	NOT NORMAL SUBGROUP OF ≡ 22B2 ⊈ 0338 ∅
22EB	⊉	DOES NOT CONTAIN AS NORMAL SUBGROUP ≡ 22B3 ⊉ 0338 ∅
22EC	⊊	NOT NORMAL SUBGROUP OF OR EQUAL TO ≡ 22B4 ⊊ 0338 ∅
22ED	⊋	DOES NOT CONTAIN AS NORMAL SUBGROUP OR EQUAL ≡ 22B5 ⊋ 0338 ∅
22EE	:	VERTICAL ELLIPSIS • these four ellipses are used for matrix row/column elision → 2026 ... horizontal ellipsis
22EF	⋯	MIDLINE HORIZONTAL ELLIPSIS
22F0	⋱	UP RIGHT DIAGONAL ELLIPSIS
22F1	⋴	DOWN RIGHT DIAGONAL ELLIPSIS
22F2	⊍	ELEMENT OF WITH LONG HORIZONTAL STROKE
22F3	⊎	ELEMENT OF WITH VERTICAL BAR AT END OF HORIZONTAL STROKE
22F4	⊏	SMALL ELEMENT OF WITH VERTICAL BAR AT END OF HORIZONTAL STROKE
22F5	⊐	ELEMENT OF WITH DOT ABOVE
22F6	⊑	ELEMENT OF WITH OVERBAR
22F7	⊒	SMALL ELEMENT OF WITH OVERBAR
22F8	⊓	ELEMENT OF WITH UNDERBAR
22F9	⊔	ELEMENT OF WITH TWO HORIZONTAL STROKES
22FA	⊕	CONTAINS WITH LONG HORIZONTAL STROKE
22FB	⊖	CONTAINS WITH VERTICAL BAR AT END OF HORIZONTAL STROKE
22FC	⊗	SMALL CONTAINS WITH VERTICAL BAR AT END OF HORIZONTAL STROKE
22FD	⊘	CONTAINS WITH OVERBAR
22FE	⊙	SMALL CONTAINS WITH OVERBAR
22FF	⊚	Z NOTATION BAG MEMBERSHIP