

Musterlösung Gruppe A

1.1	$f(x) = ax^4 + c x^2 + e$ (wegen Symmetrie) $f(0) = 0 \Rightarrow e=0$ $f(2) = -0,5 \Rightarrow 16a + 4c = -0,5$ (I) $f'(2) = 0 \quad f'(x) = 4ax^3 + 2cx$ also $32a + 4c = 0$ (II) (I) – (II) $-16a = -0,5 \Rightarrow a = \frac{1}{32}$ $c = -8 a = -\frac{1}{4}$																				
1.2	$f'(x) = \frac{1}{8}x^3 - \frac{1}{2}x \quad f''(x) = \frac{3}{8}x^2 - \frac{1}{2}$ $f''(2) = \frac{3}{2} - \frac{1}{2} > 0$ also TP																				
1.3	<table border="1"><tr><td>x</td><td>-4</td><td>-3</td><td>-2</td><td>-1</td><td>0</td><td>1</td><td>2</td><td>3</td><td>4</td></tr><tr><td>f(x)</td><td>4</td><td>0,28</td><td>-0,5</td><td>-0,2</td><td>0</td><td>-0,2</td><td>-0,5</td><td>0,28</td><td>4</td></tr></table> Graph: 	x	-4	-3	-2	-1	0	1	2	3	4	f(x)	4	0,28	-0,5	-0,2	0	-0,2	-0,5	0,28	4
x	-4	-3	-2	-1	0	1	2	3	4												
f(x)	4	0,28	-0,5	-0,2	0	-0,2	-0,5	0,28	4												
1.4.1	Sei $g_1(x) = f(x)$ für $x \in \mathbb{R}$ und $g_2(x) = 6x - 20$ für $x \in \mathbb{R}$ dann gilt: $g_1(4) = 4 \quad g_2(4) = 4$ also stetig $g_1'(x) = \frac{1}{8}x^3 - \frac{1}{2}x$ also $g_1'(4) = 8-2 = 6$ und $g_2'(4) = 6$ also diffbar.																				
1.4.2	$Q(4/4)$ und nicht $m = 6$ also z.B. $m = 0 \Rightarrow y = 4$																				
2.1	$b + h = 28 \Rightarrow h = 28 - b$ $A(b,h) = (b-6)(h-4)$ also $A(b) = (b-6)(24-b) = -b^2 + 30b - 144$ $D_A =]6; 24[$																				
2.2	$A'(b) = 30 - 2b = 0 \Rightarrow b = 15$ und $h = 13$ $A''(b) = -2 < 0 \Rightarrow \text{Max.}$																				